

RAMAKRISHNA MISSION VIDYAMANDIRA

(Residential Autonomous College affiliated to University of Calcutta)

B.A./B.Sc. THIRD SEMESTER EXAMINATION, DECEMBER 2017

SECOND YEAR [BATCH 2016-19]

PHYSICS [Honours]

Paper : III

Date : 12/12/2017

Time : 11 am – 3 pm

Full Marks : 100

Group – A

(Answer any three questions)

[3×10]

1. a) Define the electrostatic energy. Derive an expression of the electrostatic energy of a point charge distribution. [1+3]
b) Find an expression for electrostatic energy in a region of space where the field is $\vec{E}$ and permittivity of space is ϵ . Three point charges are located at three vertices of an equilateral triangle of side a . Assuming the magnitude of charge q find the electrostatic energy of the system. [3+1]
c) Find the energy of uniformly charged spherical shell of total charge q and radius R . [2]
2. a) Consider a uniformly charged sphere of radius a and charge density ρ . Show that the electric potential ϕ at any internal point with distance r from centre is given by $\phi(r) = \frac{\rho a^3}{6\epsilon_0} \left(3 - \frac{r^2}{a^2} \right)$. [3]
b) Consider a spherical shell carrying a total charge Q is cut into two equal halves. What is the force of repulsion between the two halves. [4]
c) Determine the polar equation of a equipotential surface for a dipole. [3]
3. a) Show that the electrostatic potential due to an arbitrary charge distribution may be considered as the sum of potentials due to a monopole, a dipole, a quadrupole and higher order multipoles. [4]
b) Show that if the total charge vanishes, the dipole moment is independent of the choice of origin. [2]
c) Three point charges $-q(-a, 0, 0)$, $+2q(0, 0, 0)$ and $-q(a, 0, 0)$ are placed on x-axis at the locations mentioned. Find an expression for the quadrupole moment for the given charge distribution. Hence find the potential for the system at any point $P(r, \theta)$. [3+1]
4. a) Establish the relation $\vec{D} = \epsilon_0 \vec{E} + \vec{P}$ for a parallel plate capacitor with linear dielectric within it. (Symbols have their usual meaning). [3]
b) At the plane interface between two dielectrics with $K_1 = 3$ and $K_2 = 2$, electric field $E_1 = 1200 \text{ V/m}$ in the upper medium makes an angle $\theta_1 = 45^\circ$ with the normal to the interface. Find the electric field in the lower medium and also the polarization charge density on the interface. [4]
c) A metal sphere of radius a carries a charge Q . It is surrounded out to radius b , by linear dielectric material of permittivity ϵ . Find the potential at the centre of the sphere. [3]
5. a) Consider a point charge q is placed at the front of a conducting sphere of radius a at a distance d . Calculate the induced charge density on the surface of the sphere. [4]
b) Show that the ratio of charge densities at two extreme ends ($\theta = 0^\circ$ and $\theta = 180^\circ$) of the sphere is $\frac{\sigma_1}{\sigma_2} = \left(\frac{d+a}{d-a} \right)^3$. [2]
c) The potential $V_0(\theta)$ is specified on the surface of a hollow sphere of radius R . Find the potential inside the sphere. [Assume the solution of Laplace's equation if necessary] [4]

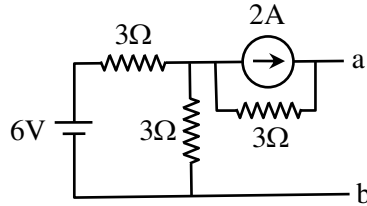
Group – B

(Answer any four questions)

[4×10]

6. a) What is magnetic vector potential? Is the choice of magnetic vector potential unique? Justify. [1+2]
 b) An electron moves in a circular orbit of radius 5.1 nm around a nucleus at a frequency of 6.8×10^{15} Hz. Find the magnetic field at the centre of the nucleus. [2]
 c) A standard solenoid of length 1m and radius 3 cm has 1000 turns is carrying current of 500mA along $\hat{\phi}$. Find the magnetic field at (i) (0,0,0) cm, (ii) (25,0,0)cm and (iii) (100,0,0)cm. [5]

7. a) Express the principle of conservation of charge in differential form. [4]
 b) In the following circuit, a load R is connected between the terminals ab. What should be the value of R such that maximum power is dissipated in it. Also, find the maximum power. [1+3]



- c) Discuss the analogy between electric and magnetic circuits. [2]
8. a) An infinite current sheet of infinitesimal thickness lies in the $z = 0$ plane with surface current density $\vec{K} = K\hat{x}$. Show that the magnetic field can be written as

$$\vec{B} = \begin{cases} -\frac{\mu_0}{2} K\hat{y} & \text{for } z > 0 \\ +\frac{\mu_0}{2} K\hat{y} & \text{for } z < 0 \end{cases}$$

Hence deduce the magnetic vector potential. [4+2]

- b) Find an expression for torque acting on a square current coil placed in a uniform magnetic field. [4]
9. a) Explain what do you mean by free current and bound current in connection with magnetization of matter. [1]
 b) Show that magnetic field due to an object of magnetization $\vec{M}$ is equivalent to sum of bound current densities $\vec{K}_b = \vec{M} \times \hat{n}$ on the surface and $\vec{J}_b = \nabla \times \vec{M}$ within the volume of the object. [5]
 c) In a magnetic material for which $\mu = 5.5\mu_0$ and $\vec{B} = 2\hat{x} + 10\hat{y} - 4\hat{z}$ mWb.m⁻². Find (i) the magnetization M, (ii) the bound current density and conduction current density, (iii) the surface current density. [1+1+2]

10. a) Two magnetic media of relative permeability μ_1 and μ_2 are separated by a plane interface. Show normal component of B field satisfy the relation $B_{1n} = B_{2n}$. [3]
 b) Show that magnetic scalar potential satisfied Laplace's equation in absence of conduction current in a material of uniform magnetization. [3]
 c) The toroid of iron ($\mu_r = 5000$) having mean diameter 20 cm and cross sectional area π cm² to produce a flux of 12.57×10^{-4} Wb in the ring. If a air gap of 8mm length is cut in the ring then calculate the current required to maintain the same flux. [The number of turns of the wire is 400]. [4]

11. a) A DC emf is applied to a circuit consisting of resistor R and a inductor L in series. Find the instantaneous current in the circuit. Show graphically how two voltages across L and R vary with time. [3+2]

- b) Calculate the self inductance (internal inductance) per unit length of a solid cylindrical conductor of radius a . [3]
- c) A solid cylindrical conductor of length 1m, radius 5cm carrying current 1A with uniform current distribution over its cross-section. Find the energy stored only within the material of the conductor. Assume the permeability of the material to be equal to μ_0 . [2]
12. a) State Faraday's law of induction. Express the integral and differential form of Faraday's law of induction and explain their significance. [1+3]
- b) A metal rod of length ℓ is placed on two rails with one end is connected with conducting wire. A uniform magnetic field B is applied perpendicular to the plane of the rail. The rod is given a push towards right with velocity v_0 . The rod moves on rails. Assume that there is no friction, find the distance before which the rod comes to rest. [3]
- c) Prove the Neumann's formula for the mutual inductance for two arbitrary loops. [3]

Group – C

(Answer any three questions)

[3×10]

13. a) Five independent shots are fired at a target. The probability of a hit in each shot is 0.25. Three hits suffice to destroy the target. Determine the probability of target destruction. [4]
- b) What do you mean by most probable macrostate? What is its role in determining the behaviour of a system in equilibrium? [2]
- c) Write down the expression of partition function (Z) of a system in thermal equilibrium at a temperature T . What is its significance? How can it be used to find the mean energy of the system? [1+1+2]
14. a) What are virial coefficients? Write down vander Waal's equation of state. Hence find virial coefficients. Find the expression for Boyle temperature in terms of virial coefficient a and b of vander Waal's gas? Show that vander Waal gas differ from ideal gas by 62.5%? [1+1+2+1+2]
- b) What is the mean inter molecular separation and the mean free path in a van der Waals gas at its critical point? Express your answers in terms of the molecular diameter d . [3]
15. a) Write down the expression of coefficient of viscosity (η) of an ideal gas. Show that $\eta \propto \frac{1}{d^2}$, where d is the molecular diameter. [2]
- b) Define the coefficient of self diffusion (D) for an ideal gas in which concentration gradient exists only along one direction. Write down the expression of D and relate it with η . [3]
- c) Deduce the expression of molecular effusion and obtain the nature of speed distribution of molecules effusing through the hole. [3+2]
16. a) Explain the thermodynamic limit. What is the importance of thermodynamic limit? [2]
- b) Find the expression for average velocity, root mean square velocity and most probable velocity according to Maxwell's velocity distribution. [2+2+2]
- c) "Atmosphere has no sharp boundaries". Explain. [1]
- d) Explain the absence of hydrogen (H_2) gas in Earth's atmosphere. [1]
17. a) Explain the difference between thermal conductivity and thermometric conductivity with example. [3]
- b) Deduce an expression for the rate of radial flow of heat under steady state per unit length of an infinite annular conducting cylinder heated uniformly along the axis. [4]
- c) The temperature of H_2 and He mixture is $T = 300K$. At what value of molecular velocity v will the Maxwell distribution function $F(v)$ yield the same magnitude for both gases. [3]

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